

Particle Movement FRQs

- 2. Stephen swims back and forth along a straight path in a 50-meter-long pool for 90 seconds. Stephen's velocity is modeled by $v(t) = 2.38e^{-0.02t}\sin\left(\frac{\pi}{56}t\right)$, where t is measured in seconds and v(t) is measured in meters per second.
 - (a) Find all times t in the interval 0 < t < 90 at which Stephen changes direction. Give a reason for your answer.

(b) Find Stephen's acceleration at time t = 60 seconds. Show the setup for your calculations, and indicate units of measure. Is Stephen speeding up or slowing down at time t = 60 seconds? Give a reason for your answer.

(c) Find the distance between Stephen's position at time $t = 20$ seconds and his position at time $t = 80$
seconds. Show the setup for your calculations.
(d) Find the total distance Stephen swims over the time interval $0 \le t \le 90$ seconds. Show the setup for your calculations.
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6. Particle P moves along the x-axis such that, for time t > 0, its position is given by $x_P(t) = 6 - 4e^{-t}$.

Particle Q moves along the y-axis such that, for time t > 0, its velocity is given by $v_Q(t) = \frac{1}{t^2}$. At time t = 1, the position of particle Q is $y_Q(1) = 2$.

(a) Find $v_P(t)$, the velocity of particle P at time t.

(b) Find $a_Q(t)$, the acceleration of particle Q at time t. Find all times t, for t > 0, when the speed of particle Q is decreasing. Justify your answer.

(c) Find $y_Q(t)$, the position of particle Q at time t .
(d) As $t \to \infty$, which particle will eventually be farther from the origin? Give a reason for your answer.
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2. A particle, P, is moving along the x-axis. The velocity of particle P at time t is given by $v_P(t) = \sin(t^{1.5})$ for $0 \le t \le \pi$. At time t = 0, particle P is at position x = 5.

A second particle, Q, also moves along the x-axis. The velocity of particle Q at time t is given by $v_Q(t) = (t - 1.8) \cdot 1.25^t$ for $0 \le t \le \pi$. At time t = 0, particle Q is at position x = 10.

(a) Find the positions of particles P and Q at time t = 1.

(b) Are particles P and Q moving toward each other or away from each other at time t = 1? Explain your reasoning.

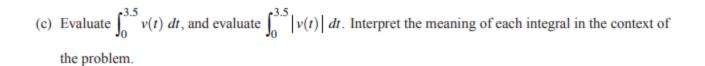
(c) Find the acceleration of particle Q at time $t = 1$. Is the speed of particle Q increasing or decreasing at
time $t = 1$? Explain your reasoning.
(d) Find the total distance traveled by particle P over the time interval $0 \le t \le \pi$.
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2. A particle moves along the *x*-axis with velocity given by $v(t) = \frac{10\sin(0.4t^2)}{t^2 - t + 3}$ for time $0 \le t \le 3.5$.

The particle is at position x = -5 at time t = 0.

(a) Find the acceleration of the particle at time t = 3.

(b) Find the position of the particle at time t = 3.



(d) A second particle moves along the x-axis with position given by $x_2(t) = t^2 - t$ for $0 \le t \le 3.5$. At what time t are the two particles moving with the same velocity?

- 5. Two particles move along the x-axis. For $0 \le t \le 8$, the position of particle P at time t is given by $x_P(t) = \ln(t^2 2t + 10)$, while the velocity of particle Q at time t is given by $v_Q(t) = t^2 8t + 15$. Particle Q is at position x = 5 at time t = 0.
 - (a) For $0 \le t \le 8$, when is particle *P* moving to the left?

(b) For $0 \le t \le 8$, find all times t during which the two particles travel in the same direction.

(c) Find the acceleration of particle Q at time t = 2. Is the speed of particle Q increasing, decreasing, or neither at time t = 2? Explain your reasoning.	
(d) Find the position of particle Q the first time it changes direction.	
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- 2. For $t \ge 0$, a particle moves along the *x*-axis. The velocity of the particle at time *t* is given by $v(t) = 1 + 2\sin\left(\frac{t^2}{2}\right)$. The particle is at position x = 2 at time t = 4.
 - (a) At time t = 4, is the particle speeding up or slowing down?

(b) Find all times t in the interval 0 < t < 3 when the particle changes direction. Justify your answer.

(c) Find the position of the particle at time $t = 0$.
(d) Find the total distance the particle travels from time $t = 0$ to time $t = 3$.
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- 2. A particle moves along a straight line. For $0 \le t \le 5$, the velocity of the particle is given by $v(t) = -2 + (t^2 + 3t)^{6/5} t^3$, and the position of the particle is given by s(t). It is known that s(0) = 10.
 - (a) Find all values of t in the interval $2 \le t \le 4$ for which the speed of the particle is 2.

(b) Write an expression involving an integral that gives the position s(t). Use this expression to find the position of the particle at time t = 5.

(c) Find all times t in the interval $0 \le t \le 5$ at which the particle changes direction. Justify your answer.
(d) Is the speed of the particle increasing or decreasing at time $t = 4$? Give a reason for your answer.
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- 6. For $0 \le t \le 12$, a particle moves along the *x*-axis. The velocity of the particle at time *t* is given by $v(t) = \cos\left(\frac{\pi}{6}t\right)$. The particle is at position x = -2 at time t = 0.
 - (a) For $0 \le t \le 12$, when is the particle moving to the left?

(b) Write, but do not evaluate, an integral expression that gives the total distance traveled by the particle from time t = 0 to time t = 6.

(c) Find the acceleration of the particle at time t . Is the speed of the particle increasing, decreasing, or neither time $t = 4$? Explain your reasoning.	r at
(d) Find the position of the particle at time $t = 4$.	
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A graphing calculator is required for these problems.

- 1. For $0 \le t \le 6$, a particle is moving along the *x*-axis. The particle's position, x(t), is not explicitly given. The velocity of the particle is given by $v(t) = 2\sin\left(e^{t/4}\right) + 1$. The acceleration of the particle is given by $a(t) = \frac{1}{2}e^{t/4}\cos\left(e^{t/4}\right)$ and x(0) = 2.
 - (a) Is the speed of the particle increasing or decreasing at time t = 5.5? Give a reason for your answer.

(b) Find the average velocity of the particle for the time period $0 \le t \le 6$.

(c) Find the total distance traveled by the particle from time $t = 0$ to $t = 6$.
(d) For $0 \le t \le 6$, the particle changes direction exactly once. Find the position of the particle at that time.
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