4. Tumbleweed, commonly found in the western United States, is the dried structure of certain plants that are blown by the wind. Kochia, a type of plant that turns into tumbleweed at the end of the summer, is a problem for farmers because it takes nutrients away from soil that would otherwise go to more beneficial plants. Scientists are concerned that kochia plants are becoming resistant to the most commonly used herbicide, glyphosate. In 2014, 19.7 percent of 61 randomly selected kochia plants were resistant to glyphosate. In 2017, 38.5 percent of 52 randomly selected kochia plants were resistant to glyphosate. Do the data provide convincing statistical evidence, at the level of $\alpha=0.05$, that there has been an increase in the proportion of all kochia plants that are resistant to glyphosate?
5. The anterior cruciate ligament (ACL) is one of the ligaments that help stabilize the knee. Surgery is often recommended if the ACL is completely torn, and recovery time from the surgery can be lengthy. A medical center developed a new surgical procedure designed to reduce the average recovery time from the surgery. To test the effectiveness of the new procedure, a study was conducted in which 210 patients needing surgery to repair a torn ACL were randomly assigned to receive either the standard procedure or the new procedure.
(a) Based on the design of the study, would a statistically significant result allow the medical center to conclude that the new procedure causes a reduction in recovery time compared to the standard procedure, for patients similar to those in the study? Explain your answer.
(b) Summary statistics on the recovery times from the surgery are shown in the table.

| Type of <br> Procedure | Sample <br> Size | Mean Recovery Time <br> (days) | Standard Deviation <br> Recovery Time (days) |
| :---: | :---: | :---: | :---: |
| Standard | 110 | 217 | 34 |
| New | 100 | 186 | 29 |

Do the data provide convincing statistical evidence that those who receive the new procedure will have less recovery time from the surgery, on average, than those who receive the standard procedure, for patients similar to those in the study?
5. The table and the bar chart below summarize the age at diagnosis, in years, for a random sample of 207 men and women currently being treated for schizophrenia.

Age-Group (years)

|  | 20 to 29 | 30 to 39 | 40 to 49 | 50 to 59 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Women | 46 | 40 | 21 | 12 | 119 |
| Men | 53 | 23 | 9 | 3 | 88 |
| Total | 99 | 63 | 30 | 15 | 207 |



Do the data provide convincing statistical evidence of an association between age-group and gender in the diagnosis of schizophrenia?
**Additionally, Do 2016 Question 5 part c (unit 3 - Sampling distributions)**

## 2016 Question \#2

2. Product advertisers studied the effects of television ads on children's choices for two new snacks. The advertisers used two 30 -second television ads in an experiment. One ad was for a new sugary snack called Choco-Zuties, and the other ad was for a new healthy snack called Apple-Zuties.
For the experiment, 75 children were randomly assigned to one of three groups, A, B, or C. Each child individually watched a 30 -minute television program that was interrupted for 5 minutes of advertising. The advertising was the same for each group with the following exceptions.

- The advertising for group A included the Choco-Zuties ad but not the Apple-Zuties ad.
- The advertising for group B included the Apple-Zuties ad but not the Choco-Zuties ad.
- The advertising for group C included neither the Choco-Zuties ad nor the Apple-Zuties ad.

After the program, the children were offered a choice between the two snacks. The table below summarizes their choices.

| Group | Type of Ad | Number Who Chose <br> Choco-Zuties | Number Who Chose <br> Apple-Zuties |
| :---: | :---: | :---: | :---: |
| A | Choco-Zuties only | 21 | 4 |
| B | Apple-Zuties only | 13 | 12 |
| C | Neither | 22 | 3 |

(a) Do the data provide convincing statistical evidence that there is an association between type of ad and children's choice of snack among all children similar to those who participated in the experiment?
(b) Write a few sentences describing the effect of each ad on children's choice of snack.
4. A researcher conducted a medical study to investigate whether taking a low-dose aspirin reduces the chance of developing colon cancer. As part of the study, 1,000 adult volunteers were randomly assigned to one of two groups. Half of the volunteers were assigned to the experimental group that took a low-dose aspirin each day, and the other half were assigned to the control group that took a placebo each day. At the end of six years, 15 of the people who took the low-dose aspirin had developed colon cancer and 26 of the people who took the placebo had developed colon cancer. At the significance level $\alpha=0.05$, do the data provide convincing statistical evidence that taking a low-dose aspirin each day would reduce the chance of developing colon cancer among all people similar to the volunteers?

## 2014 Question \#5

5. A researcher conducted a study to investigate whether local car dealers tend to charge women more than men for the same car model. Using information from the county tax collector's records, the researcher randomly selected one man and one woman from among everyone who had purchased the same model of an identically equipped car from the same dealer. The process was repeated for a total of 8 randomly selected car models.

The purchase prices and the differences (woman - man) are shown in the table below. Summary statistics are also shown.

| Car model | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Women | $\$ 20,100$ | $\$ 17,400$ | $\$ 22,300$ | $\$ 32,500$ | $\$ 17,710$ | $\$ 21,500$ | $\$ 29,600$ | $\$ 46,300$ |
| Men | $\$ 19,580$ | $\$ 17,500$ | $\$ 21,400$ | $\$ 32,300$ | $\$ 17,720$ | $\$ 20,300$ | $\$ 28,300$ | $\$ 45,630$ |
| Difference | $\$ 520$ | $-\$ 100$ | $\$ 900$ | $\$ 200$ | $-\$ 10$ | $\$ 1,200$ | $\$ 1,300$ | $\$ 670$ |


|  | Mean | Standard Deviation |
| :--- | ---: | ---: |
| Women | $\$ 25,926.25$ | $\$ 9,846.61$ |
| Men | $\$ 25,341.25$ | $\$ 9,728.60$ |
| Difference | $\$ 585.00$ | $\$ 530.71$ |

Dotplots of the data and the differences are shown below.


Purchase Price (in thousands of dollars)


Do the data provide convincing evidence that, on average, women pay more than men in the county for the same car model?
4. The Behavioral Risk Factor Surveillance System is an ongoing health survey system that tracks health conditions and risk behaviors in the United States. In one of their studies, a random sample of 8,866 adults answered the question "Do you consume five or more servings of fruits and vegetables per day?" The data are summarized by response and by age-group in the frequency table below.

| Age-Group (years) | Yes | No | Total |
| :--- | :---: | :---: | :---: |
| $18-34$ | 231 | 741 | 972 |
| $35-54$ | 669 | 2,242 | 2,911 |
| 55 or older | 1,291 | 3,692 | 4,983 |
| Total | 2,191 | 6,675 | 8,866 |

Do the data provide convincing statistical evidence that there is an association between age-group and whether or not a person consumes five or more servings of fruits and vegetables per day for adults in the United States?
5. Psychologists interested in the relationship between meditation and health conducted a study with a random sample of 28 men who live in a large retirement community. Of the men in the sample, 11 reported that they participate in daily meditation and 17 reported that they do not participate in daily meditation.
The researchers wanted to perform a hypothesis test of

$$
\begin{aligned}
& \mathrm{H}_{0}: p_{m}-p_{c}=0 \\
& \mathrm{H}_{a}: p_{m}-p_{c}<0,
\end{aligned}
$$

where $\quad p_{m}$ is the proportion of men with high blood pressure among all the men in the retirement community who participate in daily meditation and $p_{c}$ is the proportion of men with high blood pressure among all the men in the retirement community who do not participate in daily meditation.
(a) If the study were to provide significant evidence against $\mathrm{H}_{0}$ in favor of $\mathrm{H}_{a}$, would it be reasonable for the psychologists to conclude that daily meditation causes a reduction in blood pressure for men in the retirement community? Explain why or why not.

The psychologists found that of the 11 men in the study who participate in daily meditation, 0 had high blood pressure. Of the 17 men who do not participate in daily meditation, 8 had high blood pressure.
(b) Let $\hat{p}_{m}$ represent the proportion of men with high blood pressure among those in a random sample of 11 who meditate daily, and let $\hat{p}_{c}$ represent the proportion of men with high blood pressure among those in a random sample of 17 who do not meditate daily. Why is it not reasonable to use a normal approximation for the sampling distribution of $\hat{p}_{m}-\hat{p}_{c}$ ?

Although a normal approximation cannot be used, it is possible to simulate the distribution of $\hat{p}_{m}-\hat{p}_{c}$. Under the assumption that the null hypothesis is true, 10,000 values of $\hat{p}_{m}-\hat{p}_{c}$ were simulated. The histogram below shows the results of the simulation.

(c) Based on the results of the simulation, what can be concluded about the relationship between blood pressure and meditation among men in the retirement community?
3. Independent random samples of 500 households were taken from a large metropolitan area in the United States for the years 1950 and 2000. Histograms of household size (number of people in a household) for the years are shown below.

(a) Compare the distributions of household size in the metropolitan area for the years 1950 and 2000.
(b) A researcher wants to use these data to construct a confidence interval to estimate the change in mean household size in the metropolitan area from the year 1950 to the year 2000. State the conditions for using a two-sample $t$-procedure, and explain whether the conditions for inference are met.
4. A survey organization conducted telephone interviews in December 2008 in which 1,009 randomly selected adults in the United States responded to the following question.

At the present time, do you think television commercials are an effective way to promote a new product?

Of the 1,009 adults surveyed, 676 responded "yes." In December 2007, 622 of 1,020 randomly selected adults in the United States had responded "yes" to the same question. Do the data provide convincing evidence that the proportion of adults in the United States who would respond "yes" to the question changed from December 2007 to December 2008 ?
5. A recent report stated that less than 35 percent of the adult residents in a certain city will be able to pass a physical fitness test. Consequently, the city's Recreation Department is trying to convince the City Council to fund more physical fitness programs. The council is facing budget constraints and is skeptical of the report. The council will fund more physical fitness programs only if the Recreation Department can provide convincing evidence that the report is true.

The Recreation Department plans to collect data from a sample of 185 adult residents in the city. A test of significance will be conducted at a significance level of $\alpha=0.05$ for the following hypotheses.

$$
\begin{aligned}
& \mathrm{H}_{0}: p=0.35 \\
& \mathrm{H}_{\mathrm{a}}: p<0.35,
\end{aligned}
$$

where $p$ is the proportion of adult residents in the city who are able to pass the physical fitness test.
(a) Describe what a Type II error would be in the context of the study, and also describe a consequence of making this type of error.
(b) The Recreation Department recruits 185 adult residents who volunteer to take the physical fitness test. The test is passed by 77 of the 185 volunteers, resulting in a p-value of 0.97 for the hypotheses stated above. If it was reasonable to conduct a test of significance for the hypotheses stated above using the data collected from the 185 volunteers, what would the $p$-value of 0.97 lead you to conclude?
(c) Describe the primary flaw in the study described in part (b), and explain why it is a concern.
**Additionally, complete 2011 \#5 part D...in unit 4 (regression lines)

## 2011 Question \#4

4. High cholesterol levels in people can be reduced by exercise, diet, and medication. Twenty middle-aged males with cholesterol readings between 220 and 240 milligrams per deciliter ( $\mathrm{mg} / \mathrm{dL}$ ) of blood were randomly selected from the population of such male patients at a large local hospital. Ten of the 20 males were randomly assigned to group A, advised on appropriate exercise and diet, and also received a placebo. The other 10 males were assigned to group B, received the same advice on appropriate exercise and diet, but received a drug intended to reduce cholesterol instead of a placebo. After three months, posttreatment cholesterol readings were taken for all 20 males and compared to pretreatment cholesterol readings. The tables below give the reduction in cholesterol level (pretreatment reading minus posttreatment reading) for each male in the study.
Group A (placebo)

| Reduction (in mg/dL) | 2 | 19 | 8 | 4 | 12 | 8 | 17 | 7 | 24 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Mean Reduction: 10.20 Standard Deviation of Reductions: 7.66
Group B (cholesterol drug)

| Reduction (in mg/dL) | 30 | 19 | 18 | 17 | 20 | -4 | 23 | 10 | 9 | 22 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Mean Reduction: 16.40 Standard Deviation of Reductions: 9.40
Do the data provide convincing evidence, at the $\alpha=0.01$ level, that the cholesterol drug is effective in producing a reduction in mean cholesterol level beyond that produced by exercise and diet?
5. A large pet store buys the identical species of adult tropical fish from two different suppliers-Buy-Rite Pets and Fish Friends. Several of the managers at the pet store suspect that the lengths of the fish from Fish Friends are consistently greater than the lengths of the fish from Buy-Rite Pets. Random samples of 8 adult fish of the species from Buy-Rite Pets and 10 adult fish of the same species from Fish Friends were selected and the lengths of the fish, in inches, were recorded, as shown in the table below.

|  | Length of Fish |  |  |  |  |  | Mean | Standard <br> Deviation |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Buy-Rite Pets <br> $\left(n_{B}=8\right)$ | 3.4 | 2.7 | 3.3 | 4.1 | 3.5 | 3.4 | 3.0 | 3.8 |  | 3.40 | 0.434 |  |
| Fish Friends <br> $\left(n_{F}=10\right)$ | 3.3 | 2.9 | 4.2 | 3.1 | 4.2 | 4.0 | 3.4 | 3.2 | 3.7 | 2.6 | 3.46 | 0.550 |

Do the data provide convincing evidence that the mean length of the adult fish of the species from Fish Friends is greater than the mean length of the adult fish of the same species from Buy-Rite Pets?

